Generative Model-Based Text-to-Speech Synthesis

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Google

Outline

Generative TTS

Generative acoustic models for parametric TTS

Hidden Markov models (HMMs) Neural networks

Beyond parametric TTS

Learned features WaveNet End-to-end

Conclusion & future topics



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Text-to-speech as sequence-to-sequence mapping

Automatic speech recognition (ASR)

ightarrow "Hello my name is Heiga Zen"

Machine translation (MT)

"Hello my name is Heiga Zen" \rightarrow "Ich heiße Heiga Zen"

Text-to-speech synthesis (TTS) "Hello my name is Heiga Zen" \rightarrow



Speech production process



Typical flow of TTS system













Sample-based, concatenative synthesis [2]





Sample-based, concatenative synthesis [2]



Model-based, generative synthesis

Probabilistic formulation of TTS

Random variables

\mathcal{X}	Speech waveforms (data)	Observed
\mathcal{W}	Transcriptions (data)	Observed
\boldsymbol{w}	Given text	Observed
x	Synthesized speech	Unobserved



Probabilistic formulation of TTS

Random variables

\mathcal{X}	Speech waveforms (data)
\mathcal{W}	Transcriptions (data)
w	Given text
x	Synthesized speech

Observed Observed Observed Unobserved

Synthesis

- Estimate posterior predictive distribution $\rightarrow p(\pmb{x} \mid \pmb{w}, \mathcal{X}, \mathcal{W})$
- Sample \bar{x} from the posterior distribution



Probabilistic formulation

Introduce auxiliary variables (representation) + factorize dependency $p(\boldsymbol{x} \mid \boldsymbol{w}, \mathcal{X}, \mathcal{W}) = \iiint \sum_{\forall \boldsymbol{l}} \sum_{\forall \mathcal{L}} \{ p(\boldsymbol{x} \mid \boldsymbol{o}) p(\boldsymbol{o} \mid \boldsymbol{l}, \lambda) p(\boldsymbol{l} \mid \boldsymbol{w}) \\ p(\mathcal{X} \mid \boldsymbol{\mathcal{O}}) p(\boldsymbol{\mathcal{O}} \mid \boldsymbol{\mathcal{L}}, \lambda) p(\lambda) p(\mathcal{L} \mid \mathcal{W}) / p(\mathcal{X}) \} d\boldsymbol{o} d\boldsymbol{\mathcal{O}} d\lambda$

where

 \mathcal{O} , o: Acoustic features \mathcal{L} , l: Linguistic features λ : Model





Approximate {sum & integral} by best point estimates (like MAP) [3]

 $p(\boldsymbol{x} \mid \boldsymbol{w}, \mathcal{X}, \mathcal{W}) \approx p(\boldsymbol{x} \mid \hat{\boldsymbol{o}})$

where

 $\{\hat{\boldsymbol{o}}, \hat{\boldsymbol{l}}, \hat{\mathcal{O}}, \hat{\mathcal{L}}, \hat{\lambda}\} = \underset{\boldsymbol{o}, \boldsymbol{l}, \mathcal{O}, \mathcal{L}, \lambda}{\arg \max} \{ p(\boldsymbol{x} \mid \boldsymbol{o}) p(\boldsymbol{o} \mid \boldsymbol{l}, \lambda) p(\boldsymbol{l} \mid \boldsymbol{w}) \\ p(\mathcal{X} \mid \mathcal{O}) p(\mathcal{O} \mid \mathcal{L}, \lambda) p(\lambda) p(\mathcal{L} \mid \mathcal{W}) \}$



 $\text{Joint} \rightarrow \text{Step-by-step maximization [3]}$



 $\text{Joint} \rightarrow \text{Step-by-step maximization [3]}$

$\hat{\mathcal{O}} = \operatorname*{argmax}_{\mathcal{O}} p(\mathcal{X} \mid \mathcal{O})$	Extract acoustic features
$\hat{\mathcal{L}} = \arg\max_{\mathcal{L}} p(\mathcal{L} \mid \mathcal{W})$	
$\hat{\lambda} = \operatorname*{argmax}_{\lambda} p(\hat{\mathcal{O}} \mid \hat{\mathcal{L}}, \lambda) p(\lambda)$	
$\hat{\boldsymbol{l}} = \arg\max_{\boldsymbol{l}} p(\boldsymbol{l} \mid \boldsymbol{w})$	
$\hat{\boldsymbol{o}} = \operatorname*{argmax}_{\boldsymbol{o}} p(\boldsymbol{o} \mid \hat{\boldsymbol{l}}, \hat{\boldsymbol{\lambda}})$	
$\bar{\boldsymbol{x}} \sim f_{\boldsymbol{x}}(\hat{\boldsymbol{o}}) = p(\boldsymbol{x} \mid \hat{\boldsymbol{o}})$	

wÔ \boldsymbol{x}

Joint \rightarrow Step-by-step maximization [3]





Joint \rightarrow Step-by-step maximization [3]



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Joint \rightarrow Step-by-step maximization [3]



 $\text{Joint} \rightarrow \text{Step-by-step maximization [3]}$



 $\text{Joint} \rightarrow \text{Step-by-step maximization [3]}$



 $\text{Joint} \rightarrow \text{Step-by-step maximization [3]}$



Representations: acoustic, linguistic, mapping

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Representation – Linguistic features





Representation – Linguistic features



\rightarrow Based on knowledge about spoken language

- Lexicon, letter-to-sound rules
- Tokenizer, tagger, parser
- Phonology rules



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Representation – Acoustic features

Piece-wise stationary, source-filter generative model $p(\boldsymbol{x} \mid \boldsymbol{o})$





Representation – Acoustic features

Piece-wise stationary, source-filter generative model $p(\boldsymbol{x} \mid \boldsymbol{o})$



\rightarrow Needs to solve inverse problem

- Estimate parameters from signals
- Use estimated parameters (e.g., cepstrum) as acoustic features



Rule-based, formant synthesis [1]

$$\hat{\mathcal{O}} = \underset{\mathcal{O}}{\operatorname{arg\,max}} p(\mathcal{X} \mid \mathcal{O}) \qquad \text{Vocoder analysis} \\ \hat{\mathcal{L}} = \underset{\mathcal{L}}{\operatorname{arg\,max}} p(\mathcal{L} \mid \mathcal{W}) \qquad \text{Text analysis} \\ \hat{\lambda} = \underset{\lambda}{\operatorname{arg\,max}} p(\hat{\mathcal{O}} \mid \hat{\mathcal{L}}, \lambda) p(\lambda) \qquad \textbf{Extract rules} \\ \hat{l} = \underset{l}{\operatorname{arg\,max}} p(l \mid w) \qquad \text{Text analysis} \\ \hat{o} = \underset{o}{\operatorname{arg\,max}} p(o \mid \hat{l}, \hat{\lambda}) \qquad \textbf{Apply rules} \\ \bar{x} \sim f_{x}(\hat{o}) = p(x \mid \hat{o}) \qquad \text{Vocoder synthesis} \end{cases}$$

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ô

 \boldsymbol{x}

 \boldsymbol{w}

Rule-based, formant synthesis [1]

$$\hat{\mathcal{O}} = \underset{\mathcal{O}}{\operatorname{arg\,max}} p(\mathcal{X} \mid \mathcal{O})$$
 Vocoder analysis

$$\hat{\mathcal{L}} = \underset{\mathcal{L}}{\operatorname{arg\,max}} p(\mathcal{L} \mid \mathcal{W})$$
 Text analysis

$$\hat{\lambda} = \underset{\lambda}{\operatorname{arg\,max}} p(\hat{\mathcal{O}} \mid \hat{\mathcal{L}}, \lambda) p(\lambda)$$
 Extract rules

$$\hat{l} = \underset{l}{\operatorname{arg\,max}} p(l \mid w)$$
 Text analysis

$$\hat{o} = \underset{o}{\operatorname{arg\,max}} p(o \mid \hat{l}, \hat{\lambda})$$
 Apply rules

$$\bar{x} \sim f_{x}(\hat{o}) = p(x \mid \hat{o})$$
 Vocoder synthesis

\rightarrow Hand-crafted rules on knowledge-based features

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Generative Model-Based Text-to-Speech Synthesis

x

HMM-based [4], statistical parametric synthesis [5]

$$\hat{\mathcal{O}} = \underset{\mathcal{O}}{\operatorname{arg\,max}} p(\mathcal{X} \mid \mathcal{O})$$
 Vocoder analysis

$$\hat{\mathcal{L}} = \underset{\mathcal{L}}{\operatorname{arg\,max}} p(\mathcal{L} \mid \mathcal{W})$$
 Text analysis

$$\hat{\lambda} = \underset{\lambda}{\operatorname{arg\,max}} p(\hat{\mathcal{O}} \mid \hat{\mathcal{L}}, \lambda) p(\lambda)$$
 Train HMMs

$$\hat{l} = \underset{l}{\operatorname{arg\,max}} p(l \mid w)$$
 Text analysis

$$\hat{o} = \underset{o}{\operatorname{arg\,max}} p(o \mid \hat{l}, \hat{\lambda})$$
 Parameter generation

$$\bar{x} \sim f_{x}(\hat{o}) = p(x \mid \hat{o})$$
 Vocoder synthesis

$$\hat{\mathcal{O}} = \underset{o}{\underset{o}{\mathcal{L}}} \hat{l}$$

 \boldsymbol{x}

HMM-based [4], statistical parametric synthesis [5]



\rightarrow Replace rules by HMM-based generative acoustic model

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HMM-based generative acoustic model for TTS

- Context-dependent subword HMMs
- Decision trees to cluster & tie HMM states \rightarrow interpretable



$$\begin{split} p(\boldsymbol{o} \mid \boldsymbol{l}, \lambda) &= \sum_{\forall \boldsymbol{q}} \prod_{t=1}^{T} p(\boldsymbol{o}_t \mid q_t, \lambda) P(\boldsymbol{q} \mid \boldsymbol{l}, \lambda) \quad q_t \text{: hidden state at } t \\ &= \sum_{\forall \boldsymbol{q}} \prod_{t=1}^{T} \mathcal{N}(\boldsymbol{o}_t; \boldsymbol{\mu}_{q_t}, \boldsymbol{\Sigma}_{q_t}) P(\boldsymbol{q} \mid \boldsymbol{l}, \lambda) \end{split}$$

HMM-based generative acoustic model for TTS

- Non-smooth, step-wise statistics
 → Smoothing is essential
- Difficult to use high-dimensional acoustic features (e.g., raw spectra)
 → Use low-dimensional features (e.g., cepstra)
- Data fragmentation
 - \rightarrow Ineffective, local representation

A lot of research work have been done to address these issues



Alternative acoustic model

HMM: Handle variable length & alignment **Decision tree:** Map linguistic \rightarrow acoustic



Regression tree: linguistic features \rightarrow Stats. of acoustic features



Alternative acoustic model

HMM: Handle variable length & alignment **Decision tree:** Map linguistic \rightarrow acoustic



Regression tree: linguistic features \rightarrow Stats. of acoustic features

Replace the tree w/ a general-purpose regression model $\rightarrow \textbf{Artificial neural network}$



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FFNN-based acoustic model for TTS [6]



 $\hat{o}_t pprox \mathbb{E}\left[o_t \mid oldsymbol{l}_t
ight]
ightarrow \mathsf{Replace}$ decision trees & Gaussian distributions



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RNN-based acoustic model for TTS [7]



FFNN: $\hat{o}_t \approx \mathbb{E}[o_t | l_t]$ RNN: $\hat{o}_t \approx \mathbb{E}[o_t | l_1, \dots, l_t]$

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Generative Model-Based Text-to-Speech Synthesis

NN-based generative acoustic model for TTS

- Non-smooth, step-wise statistics \rightarrow RNN predicts smoothly varying acoustic features [7, 8]
- Difficult to use high-dimensional acoustic features (e.g., raw spectra) \rightarrow Layered architecture can handle high-dimensional features [9]
- Data fragmentation

 \rightarrow Distributed representation [10]

NN-based generative acoustic model for TTS

- Non-smooth, step-wise statistics \rightarrow RNN predicts smoothly varying acoustic features [7, 8]
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- Data fragmentation
 - \rightarrow Distributed representation [10]
- NN-based approach is now mainstream in research & products
- Models: FFNN [6], MDN [11], RNN [7], Highway network [12], GAN [13]
- Products: e.g., Google [14]



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NN-based generative model for TTS



$\mathsf{Text} \to \mathsf{Linguistic} \to (\mathsf{Articulatory}) \to \mathsf{Acoustic} \to \mathsf{Waveform}$



Generative Model-Based Text-to-Speech Synthesis

Knowledge-based features \rightarrow Learned features

Unsupervised feature learning



- Speech: auto-encoder at FFT spectra $[9, 15] \rightarrow positive results$
- Text: word [16], phone & syllable [17] \rightarrow less positive



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Relax approximation

Joint acoustic feature extraction & model training

 $\textbf{Two-step optimization} \rightarrow \textbf{Joint optimization}$

$$\begin{cases} \hat{\mathcal{O}} = \underset{\mathcal{O}}{\arg \max} p(\mathcal{X} \mid \mathcal{O}) \\ \hat{\lambda} = \underset{\lambda}{\arg \max} p(\hat{\mathcal{O}} \mid \hat{\mathcal{L}}, \lambda) p(\lambda) \\ & \downarrow \\ \{\hat{\lambda}, \hat{\mathcal{O}}\} = \underset{\lambda, \mathcal{O}}{\arg \max} p(\mathcal{X} \mid \mathcal{O}) p(\mathcal{O} \mid \hat{\mathcal{L}}, \lambda) p(\lambda) \end{cases}$$

Joint source-filter & acoustic model optimization

- HMM [18, 19, 20]
- NN [21, 22]



Relax approximation

Joint acoustic feature extracion & model training

Mixed-phase cepstral analysis + LSTM-RNN [22]





Relax approximation Direct mapping from linguistic to waveform

No explicit acoustic features

$$\begin{aligned} \{\hat{\lambda}, \hat{\mathcal{O}}\} &= \operatorname*{arg\,max}_{\lambda, \mathcal{O}} p(\mathcal{X} \mid \mathcal{O}) p(\mathcal{O} \mid \hat{\mathcal{L}}, \lambda) p(\lambda) \\ & \downarrow \\ \hat{\lambda} &= \operatorname*{arg\,max}_{\lambda} p(\mathcal{X} \mid \hat{\mathcal{L}}, \lambda) p(\lambda) \end{aligned}$$

Generative models for raw audio

- LPC [23]
- WaveNet [24]
- SampleRNN [25]



WaveNet: A generative model for raw audio

Autoregressive (AR) modelling of speech signals

$$\boldsymbol{x} = \{x_0, x_1, \dots, x_{N-1}\} \quad \text{: raw waveform}$$
$$p(\boldsymbol{x} \mid \lambda) = p(x_0, x_1, \dots, x_{N-1} \mid \lambda) = \prod_{n=0}^{N-1} p(x_n \mid x_0, \dots, x_{n-1}, \lambda)$$



WaveNet: A generative model for raw audio

Autoregressive (AR) modelling of speech signals

$$\boldsymbol{x} = \{x_0, x_1, \dots, x_{N-1}\} \quad \text{: raw waveform}$$
$$p(\boldsymbol{x} \mid \lambda) = p(x_0, x_1, \dots, x_{N-1} \mid \lambda) = \prod_{n=0}^{N-1} p(x_n \mid x_0, \dots, x_{n-1}, \lambda)$$

WaveNet [24] $\rightarrow p(x_n \mid x_0, \dots, x_{n-1}, \lambda)$ is modeled by *convolutional NN*



WaveNet: A generative model for raw audio

Autoregressive (AR) modelling of speech signals

$$\begin{aligned} \boldsymbol{x} &= \{x_0, x_1, \dots, x_{N-1}\} \quad \text{: raw waveform} \\ p(\boldsymbol{x} \mid \lambda) &= p(x_0, x_1, \dots, x_{N-1} \mid \lambda) = \prod_{n=0}^{N-1} p(x_n \mid x_0, \dots, x_{n-1}, \lambda) \end{aligned}$$

WaveNet [24]

 $\rightarrow p(x_n \mid x_0, \dots, x_{n-1}, \lambda)$ is modeled by convolutional NN

Key components

- Causal dilated convolution: capture long-term dependency
- Gated convolution + residual + skip: powerful non-linearity
- Softmax at output: classification rather than regression



WaveNet - Causal dilated convolution

100ms in 16kHz sampling = 1,600 time steps

 \rightarrow Too long to be captured by normal RNN/LSTM

Dilated convolution

Exponentially increase receptive field size w.r.t. # of layers



WaveNet - Non-linearity



WaveNet – Softmax



Analog audio signal



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WaveNet – Softmax



Sampling & Quantization



WaveNet – Softmax



Categorical distribution \rightarrow Histogram

- Unimodal
- Multimodal
- Skewed

...





WaveNet - Conditional modelling



WaveNet vs conventional audio generative models

Assumptions in conventional audio generative models [23, 26, 27, 22]

- Stationary process w/ fixed-length analysis window \rightarrow Estimate model within 20–30ms window w/ 5–10 shift
- Linear, time-invariant filter within a frame
 - \rightarrow Relationship between samples can be non-linear
- Gaussian process
 - \rightarrow Assumes speech signals are normally distributed

WaveNet

- Sample-by-saple, non-linear, capable to take additional inputs
- Arbitrary-shaped signal distribution

SOTA subjective naturalness w/ WaveNet-based TTS [24] HMM () LSTM () Concatenative () WaveNet ()



Relax approximation Towards Bayesian end-to-end TTS

Integrated end-to-end

$$\begin{cases} \hat{\mathcal{L}} = \arg \max_{\mathcal{L}} p(\mathcal{L} \mid \mathcal{W}) \\ \hat{\lambda} = \arg \max_{\lambda} p(\mathcal{X} \mid \hat{\mathcal{L}}, \lambda) p(\lambda) \\ & \downarrow \\ \hat{\lambda} = \arg \max_{\lambda} p(\mathcal{X} \mid \mathcal{W}, \lambda) p(\lambda) \end{cases}$$

Text analysis is integrated to model



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Relax approximation Towards Bayesian end-to-end TTS

Bayesian end-to-end

$$\begin{cases} \hat{\lambda} = \underset{\lambda}{\arg \max} p(\mathcal{X} \mid \mathcal{W}, \lambda) p(\lambda) \\ \bar{x} \sim f_{x}(\boldsymbol{w}, \hat{\lambda}) = p(\boldsymbol{x} \mid \boldsymbol{w}, \hat{\lambda}) \\ & \downarrow \\ \bar{x} \sim f_{x}(\boldsymbol{w}, \mathcal{X}, \mathcal{W}) = p(\boldsymbol{x} \mid \boldsymbol{w}, \mathcal{X}, \mathcal{W}) \\ = \int p(\boldsymbol{x} \mid \boldsymbol{w}, \lambda) p(\lambda \mid \mathcal{X}, \mathcal{W}) d\lambda \\ \approx \frac{1}{K} \sum_{k=1}^{K} p(\boldsymbol{x} \mid \boldsymbol{w}, \hat{\lambda}_{k}) \quad \leftarrow \text{Ensemble} \end{cases}$$



Marginalize model parameters & architecture



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Generative model-based text-to-speech synthesis

- Bayes formulation + factorization + approximations
- Representation: acoustic features, linguistic features, mapping
 - Mapping: Rules \rightarrow HMM \rightarrow NN
 - $-\,$ Feature: Engineered \rightarrow Unsupervised, learned
- Less approximations
 - Joint training, direct waveform modelling
 - Moving towards integrated & Bayesian end-to-end TTS

Naturalness: Concatenative \leq Generative

 $\textbf{Flexibility:} \ Concatenative \ll \textit{Generative} \ (e.g., multiple \ speakers)$



Beyond "text"-to-speech synthesis

TTS on conversational assistants

- Texts aren't fully contained
- Need more context
 - Location to resolve homographs
 - User query to put right emphasis





Beyond "text"-to-speech synthesis

TTS on conversational assistants

- Texts aren't fully contained
- Need more context
 - Location to resolve homographs
 - User query to put right emphasis



We need representation that can

organize the world information & make it accessible & useful

from TTS generative models ©



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Beyond "generative" TTS

Generative model-based TTS

- Model represents process behind speech production
 - Trained to minimize error against human-produced speech
 - Learned model \rightarrow *speaker*



Beyond "generative" TTS

Generative model-based TTS

- Model represents process behind speech production
 - Trained to minimize error against human-produced speech
 - Learned model $\rightarrow \textit{speaker}$
- Speech is for communication
 - Goal: maximize the amount of information to be received

Missing "listener"

 \rightarrow "listener" in training / model itself?



Thanks!





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